Lesson 6: Area in the Real World

Student Outcomes

- Students determine the area of composite figures in real-life contextual situations using composition and decomposition of polygons.
- Students determine the area of a missing region using composition and decomposition of polygons.

Lesson Notes

Finding area in real-world contexts can be done around the classroom, in a hallway, or in different locations around the school. This lesson requires the teacher to measure and record the dimensions of several objects and calculate the area ahead of time. Choices are dependent on time available and various students’ needs. Different levels of student autonomy can be taken into account when grouping and deciding which objects to measure. Further, the measurement units and precision can be adjusted to students’ ability level.

Floor tile, carpet area, walls, and furniture in the classroom can be used for this lesson. Smaller objects within the classroom may also be used, such as bulletin boards, notebooks, windows, and file cabinets. Exploring the school building for other real-world area problems might lead to a stage in an auditorium or walkway around a school pool. Of course, adhere to school policy regarding supervision of students, and be vigilant about safety. Students should not have to climb to make measurements.

Throughout the lesson, there are opportunities to compare unsimplified numerical expressions. These are important and should be emphasized because they help prepare students for algebra.

Classwork

Gauge students’ ability level regarding which units and level of precision will be used in this lesson. Using metric units for length and height of the classroom wall most likely requires measuring to the nearest 0.1 meter or 0.01 meter and multiplying decimals to calculate area. Choosing standard units allows precision to be set to the nearest foot, half foot, etc., but it could require multiplying fractional lengths.

Discussion (5 minutes)

Decide whether the whole group stays in the classroom or if carefully selected groups are sent out on a measurement mission to somewhere outside the classroom. All students should understand which measurement units to use and to what precision they are expected to measure.

- Area problems in the real world are all around us. Can you give an example of when you might need to know the area of something?
  - Area needs to be considered when covering an area with paint, carpet, tile, or wallpaper; wrapping a present; etc.

Scaffolding:

As noted in the classwork section, there is great flexibility in this lesson, so it can be tailored to the needs of the class and can be easily individualized for both struggling and advanced learners. English language learners might need a mini-lesson on the concept of wallpaper with accompanying visuals and video, if possible.
The Problem Set from the last lesson had a wall that was to be painted. What measurement units were used in that problem?

- All linear measurements were made in feet. Paint was calculated in quarts.

How precisely were the measurements made?

- Measurements were most likely measured to the nearest foot. Paint was rounded up to the next quart.

Could those measurements have been made more precisely?

- Yes, measurements could have been made to the nearest inch, half inch, or some other smaller fraction of an inch. Paint can be purchased in pints.

We can measure the dimensions of objects and use those measurements to calculate the surface area of the object. Our first object will be a wall in this classroom.

Exploratory Challenge 1 (34 minutes): Classroom Wall Paint

The custodians are considering painting our classroom next summer. In order to know how much paint they must buy, the custodians need to know the total surface area of the walls. Why do you think they need to know this, and how can we find the information?

All classroom walls are different. Taking overall measurements and then subtracting windows, doors, or other areas will give a good approximation.

Make a prediction of how many square feet of painted surface there are on one wall in the room. If the floor has square tiles, these can be used as a guide.

Students make a prediction of how many square feet of painted surface there are on one wall in the room. If the floor has square tiles, these can be used as a guide.

Estimate the dimensions and area. Predict the area before you measure. My prediction: ________ ft².

- Measure and sketch one classroom wall. Include measurements of windows, doors, or anything else that would not be painted.

**Student responses will depend on the teacher’s choice of wall.**

<table>
<thead>
<tr>
<th>Object or Item to Be Measured</th>
<th>Measurement Units</th>
<th>Precision (measure to the nearest)</th>
<th>Length</th>
<th>Width</th>
<th>Expression That Shows the Area</th>
<th>Area</th>
</tr>
</thead>
<tbody>
<tr>
<td>Door</td>
<td>feet</td>
<td>half foot</td>
<td>6 (\frac{1}{2}) ft.</td>
<td>3 (\frac{1}{2}) ft.</td>
<td>6 (\frac{1}{2}) ft. × 3 (\frac{1}{2}) ft.</td>
<td>22 (\frac{3}{4}) ft²</td>
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</tbody>
</table>
b. Work with your partners and your sketch of the wall to determine the area that needs paint. Show your sketch and calculations below; clearly mark your measurements and area calculations.

c. A gallon of paint covers about 350 ft$^2$. Write an expression that shows the total area of the wall. Evaluate it to find how much paint is needed to paint the wall.

*Answers will vary based on the size of the wall. Fractional answers are to be expected.*

d. How many gallons of paint would need to be purchased to paint the wall?

*Answers will vary based on the size of the wall. The answer from part (d) should be an exact quantity because gallons of paint are discrete units. Fractional answers from part (c) must be rounded up to the nearest whole gallon.*

### Exploratory Challenge 2 (Optional—15 minutes)

Assign other walls in the classroom for groups to measure and calculate the area, or send some students to measure and sketch other real-world area problems found around the school. The teacher should measure the objects prior to the lesson using the same units and precision students are using. Objects may have to be measured multiple times if the activity has been differentiated using different units or levels of precision.

<table>
<thead>
<tr>
<th>Object or Item to Be Measured</th>
<th>Measurement Units</th>
<th>Precision (measure to the nearest)</th>
<th>Length</th>
<th>Width</th>
<th>Area</th>
</tr>
</thead>
<tbody>
<tr>
<td>Door</td>
<td>feet</td>
<td>half foot</td>
<td>$1\frac{1}{2}$ ft</td>
<td>$\frac{3}{2}$ ft</td>
<td>$22\frac{3}{4}$ ft$^2$</td>
</tr>
</tbody>
</table>

### Closing (3 minutes)

- What real-life situations require us to use area?
  - *Floor covering, like carpets and tiles, require area measurements. Wallpaper and paint also call for area measurements. Fabric used for clothing and other items also demand that length and width be considered. Wrapping a present; installing turf on a football field; or laying bricks, pavers, or concrete for a deck or patio are other real-world examples.*

- Sometimes measurements are given in inches and area is calculated in square feet. How many square inches are in a square foot?
  - *There are 144 square inches in a square foot, 12 in. $\times$ 12 in. = 144 in$^2$.***

### Exit Ticket (3 minutes)
Lesson 6: Area in the Real World

Exit Ticket

Find the area of the deck around this pool. The deck is the white area in the diagram.

[Diagram showing a rectangle with dimensions 50 m x 90 m, 15 m x 25 m]
Exit Ticket Sample Solutions

Find the area of the deck around this pool. The deck is the white area in the diagram.

Area of Walkway and Pool: $A = bh$
- $A = 90 \text{ m} \times 25 \text{ m}$
- $A = 2,250 \text{ m}^2$

Area of Pool: $A = bh$
- $A = 50 \text{ m} \times 15 \text{ m}$
- $A = 750 \text{ m}^2$

Area of Walkway: $2,250 \text{ m}^2 - 750 \text{ m}^2 = 1,500 \text{ m}^2$

Problem Set Sample Solutions

1. Below is a drawing of a wall that is to be covered with either wallpaper or paint. The wall is 8 ft. high and 16 ft. wide. The window, mirror, and fireplace are not to be painted or papered. The window measures 18 in. wide and 14 ft. high. The fireplace is 5 ft. wide and 3 ft. high, while the mirror above the fireplace is 4 ft. wide and 2 ft. high. (Note: this drawing is not to scale.)

a. How many square feet of wallpaper are needed to cover the wall?

Total wall area = 8 ft. × 16 ft. = 128 ft$^2$
Window area = 14 ft. × 1.5 ft. = 21 ft$^2$
Fireplace area = 3 ft. × 5 ft. = 15 ft$^2$
Mirror area = 4 ft. × 2 ft. = 8 ft$^2$
Net wall area to be covered = $128 \text{ ft}^2 - (21 \text{ ft}^2 + 15 \text{ ft}^2 + 8 \text{ ft}^2) = 84 \text{ ft}^2$
b. The wallpaper is sold in rolls that are 18 in. wide and 33 ft. long. Rolls of solid color wallpaper will be used, so patterns do not have to match up.
   i. What is the area of one roll of wallpaper?
   
   \[ \text{Area of one roll of wallpaper: } 33 \text{ ft.} \times 1.5 \text{ ft.} = 49.5 \text{ ft}^2 \]
   
   ii. How many rolls would be needed to cover the wall?
   
   \[ 84 \text{ ft}^2 \div 49.5 \text{ ft}^2 = 1.7; \text{ therefore, 2 rolls would need to be purchased.} \]

   c. This week, the rolls of wallpaper are on sale for $11.99/roll. Find the cost of covering the wall with wallpaper.

   \[ \text{We need two rolls of wallpaper to cover the wall, which will cost } $11.99 \times 2 = $23.98. \]

d. A gallon of special textured paint covers 200 ft\(^2\) and is on sale for $22.99/gallon. The wall needs to be painted twice (the wall needs two coats of paint). Find the cost of using paint to cover the wall.

   \[ \text{Total wall area} = 8 \text{ ft.} \times 16 \text{ ft.} = 128 \text{ ft}^2 \]
   \[ \text{Window area} = 14 \text{ ft.} \times 1.5 \text{ ft.} = 21 \text{ ft}^2 \]
   \[ \text{Fireplace area} = 3 \text{ ft.} \times 5 \text{ ft.} = 15 \text{ ft}^2 \]
   \[ \text{Mirror area} = 4 \text{ ft.} \times 2 \text{ ft.} = 8 \text{ ft}^2 \]
   \[ \text{Net wall area to be covered} = 128 \text{ ft}^2 - (21 \text{ ft}^2 + 15 \text{ ft}^2 + 8 \text{ ft}^2) = 84 \text{ ft}^2 \]

   If the wall needs to be painted twice, we need to paint a total area of \(84 \text{ ft}^2 \times 2 = 168 \text{ ft}^2\). One gallon is enough paint for this wall, so the cost will be $22.99.

2. A classroom has a length of 30 ft. and a width of 20 ft. The flooring is to be replaced by tiles. If each tile has a length of 36 in. and a width of 24 in., how many tiles are needed to cover the classroom floor?

   \[ \text{Area of the classroom: } 30 \text{ ft.} \times 20 \text{ ft.} = 600 \text{ ft}^2 \]
   \[ \text{Area of each tile: } 3 \text{ ft.} \times 2 \text{ ft.} = 6 \text{ ft}^2 \]

   \[ \frac{\text{Area of the classroom}}{\text{Area of each tile}} = \frac{600 \text{ ft}^2}{6 \text{ ft}^2} = 100 \]

   100 tiles are needed to cover the classroom floor. Allow for students who say that if the tiles are 3 ft. \(\times\) 2 ft., and they orient them in a way that corresponds to the 30 ft. \(\times\) 20 ft. room, then they will have ten rows of ten tiles giving them 100 tiles. Using this method, the students do not need to calculate the areas and divide. Orienting the tiles the other way, students could say that they will need 105 tiles as they will need \(\frac{2}{3}\) rows of 15 tiles, and since \(\frac{2}{3}\) of a tile cannot be purchased, they will need 7 rows of 15 tiles.

3. Challenge: Assume that the tiles from Problem 2 are unavailable. Another design is available, but the tiles are square, 18 in. on a side. If these are to be installed, how many must be ordered?

   Solutions will vary. An even number of tiles fit on the 30 foot length of the room (20 tiles), but the width requires \(13 \frac{1}{3}\) tiles. This accounts for a 20 tile by 13 tile array. \(20 \times 13 = 260\). 260 tiles need to be ordered.

   The remaining area is 30 ft. \(\times\) 0.5 ft. \((20 \times \frac{1}{3}\) tile\)

   Since 20 of the \(\frac{1}{3}\) tiles are needed, 7 additional tiles must be cut to form \(\frac{21}{3}\). 20 of these will be used with \(\frac{1}{3}\) of 1 tile left over.

   Using the same logic as above, some students may correctly say they will need 280 tiles.
4. A rectangular flower bed measures 10 m by 6 m. It has a path 2 m wide around it. Find the area of the path.

![Diagram of a flower bed with a path around it]

- **Total area**: $14 \times 10 = 140 \text{ m}^2$
- **Flower bed area**: $10 \times 6 = 60 \text{ m}^2$
- **Area of path**: $140 \text{ m}^2 - 60 \text{ m}^2 = 80 \text{ m}^2$

5. A diagram of Tracy’s deck is shown below, shaded blue. He wants to cover the missing portion of his deck with soil in order to grow a garden.

   a. Find the area of the missing portion of the deck. Write the expression and evaluate it.

   ![Diagram of a deck with a missing portion shaded blue]

   Students should use one of two methods to find the area: finding the dimensions of the garden area (interior rectangle, $6 \times 2 \text{ m}$) or finding the total area minus the sum of the four wooden areas, shown below.

   - **$6 \times 2 = 12 \text{ m}^2$**
   - **OR**
   - **$8 \times 6 - 7 \times 3 - 5 \times 1 - 8 \times 1 - 2 \times 1 = 12 \text{ (All linear units are in meters; area is in square meters.)}$**

   b. Find the area of the missing portion of the deck using a different method. Write the expression and evaluate it.

   Students should choose whichever method was not used in part (a).
c. Write two equivalent expressions that could be used to determine the area of the missing portion of the deck.

\[ 8 \times 6 - 7 \times 3 - 5 \times 1 - 8 \times 1 - 2 \times 1 \]
\[ 6 \times 2 \]

d. Explain how each expression demonstrates a different understanding of the diagram.

One expression shows the dimensions of the garden area (interior rectangle, \(6 \times 2 \text{ m}\)), and one shows finding the total area minus the sum of the four wooden areas.

6. The entire large rectangle below has an area of \(3 \frac{1}{2} \text{ ft}^2\). If the dimensions of the white rectangle are as shown below, write and solve an equation to find the area, \(A\), of the shaded region.

\[
\frac{3}{4} \text{ft} \times \frac{3}{8} \text{ft} = \frac{9}{32} \text{ ft}^2
\]
\[
\frac{9}{32} \text{ ft}^2 + A = 3 \frac{1}{2} \text{ ft}^2
\]
\[
A = 3 \frac{7}{32} \text{ ft}^2
\]